

Energy Harvesting Wireless Sensor Networks: Delay Analysis Considering Energy Costs of Sensing and Transmission

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Abstract—Energy harvesting (EH) provides a means of greatly enhancing the lifetime of wireless sensor nodes. However, the randomness inherent in the EH process may cause significant delay for performing sensing operations and transmitting sensed information to the sink. Unlike most existing studies on the delay performance of EH sensor networks, where only the energy consumption of transmission is considered, we consider the energy costs of both sensing and transmission. Specifically, we consider an EH sensor that monitors some status property and adopts a harvest-then-use protocol to perform sensing and transmission. To comprehensively study the delay performance, we consider two complementary metrics and analytically derive their statistics: 1) update age—measuring the time taken from when information is obtained by the sensor to when the sensed information is successfully transmitted to the sink, i.e., how timely the updated information at the sink is, and 2) update cycle—measuring the time duration between two consecutive successful transmissions, i.e., how frequently the information at the sink is updated. Our results show that the consideration of sensing energy cost leads to an important tradeoff between the two metrics: more frequent updates result in less timely information available at the sink.

Index Terms—Energy harvesting, wirelessly powered communications, delay analysis, energy costs of sensing and transmission.

I. INTRODUCTION

BACKGROUND: Energy harvesting (EH) from energy sources in the ambient environment is an attractive solution to power wireless sensor networks (WSNs). The feasibility of powering WSNs by EH from solar, wind, vibration and radio-frequency (RF) signals has been demonstrated in the

literature [1]–[5]. If an EH source is periodically or continuously available, a sensor node can in theory be powered perpetually. However, the design of EH WSNs raises several interesting and challenging issues.

Design Challenges: An important design consideration for EH WSNs is the modeling of energy costs. There are three main energy costs in wireless sensors [6]: (i) energy cost of RF transmission and reception, including idle listening, (ii) energy cost of information sensing and processing, and (iii) energy cost of other basic processing while being active. Generally, the energy cost of other basic processing is much smaller compared to the energy cost of transmission [7]. Hence, the majority of the current work on EH WSNs has considered only the energy cost of transmission, while ignoring the energy cost of sensing [8], [9]. For some sensors, such as high-rate and high-resolution acoustic and seismic sensors, the energy cost of sensing can actually be higher than the energy cost of transmission, e.g., see [10] and references therein. Hence, it is important to accurately model the energy cost of sensing in WSNs [11].

For WSNs powered by EH from the ambient environment, the energy arrival process is inherently time-varying in nature. These fluctuations in the energy arrival process can be slow or fast and are characterised by its coherence time [12]. For instance, for the case of EH from a solar panel on a clear day with abundant sunshine, the coherence time is on the order of minutes or hours. For the case of wireless energy transfer via RF signals, the coherence time can be on the order of milliseconds, which is comparable to the duration of a communication time slot. The energy arrival process in the latter case can be modeled as a random process where the amount of harvested energy in each time slot follows some probability distribution. For example, papers studying EH from RF signals often assume an exponential distribution [13]–[15]. Another example, using the gamma distribution, can be found in [16]. However, many energy arrival processes in practice cannot be accurately modeled by using exponential or gamma distributions. The consideration of a more general probability distribution for modeling the amount of energy arrival is still largely an open problem.

In many sensor network applications, the delay performance is a key design challenge. The effects of randomness in both arrivals of the multiple data packets and harvested energy on the overall transmission completion time were considered in [17]. In [13], a single data packet and randomness in the energy arrival process and wireless channel, were considered in the

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analysis of transmission delay, i.e., the time duration between the generation of a packet and its successful reception at the sink. However, both [17] and [13] only considered the energy cost of transmission. To the best of our knowledge, a comprehensive analysis of the delay performance of EH WSNs taking into account a realistic model of sensor energy costs, has not been investigated in the literature.

Paper Contributions: We consider a status *monitoring* scenario, e.g., monitoring some property of a target environment, with one sensor-sink pair. The sensor is solely powered by EH from an ambient energy source. The sensor periodically monitors and senses the current environment, i.e., it generates current status information about one or more variables of interest, and then transmits a status-information-containing packet to the sink¹. Once the packets are successfully transmitted to the sink, which may occur after several failed retransmissions due to fading in the transmission channel, the status under monitoring is *updated* at the sink.

We adopt two different metrics to assess the delay performance: (i) update age² which measures the time duration between the time of generation of the current status information at the sink and the time at which it is updated at the sink, and (ii) update cycle which measures the time duration between one status update at the sink to the next. The update age (or freshness) and update cycle (or frequency) are complementary measures. For instance, a smaller update age means the updated status information at the sink is much more timely, but does not indicate when the next update status information will be received. A smaller update cycle means more frequent status updates at the sink, but does not indicate when the current updated status information was originally generated or how old it is. Thus, the quality of a status monitoring system, i.e., the status update freshness and frequency, is comprehensively captured by the update age and update cycle, respectively.

We account for the fact that sensing and transmission operations both consume energy. Inspired from the harvest-then-use and save-then-transmit communication protocols for EH nodes in wireless networks [13], [14], [16], which are simple to implement in practice, we consider a harvest-then-use protocol for the EH sensor. In our proposed protocol, the sensor performs sensing and transmission as soon as it has harvested sufficient energy. In order to limit the delay due to retransmissions, we impose a time window for retransmissions. The delay performance of the considered harvest-then-use protocol is analyzed. The main contributions of this paper are as follows:

- We provide a comprehensive study on the delay performance of EH sensor networks. Apart from the commonly considered delay due to the information transmission from the sensor to the sink, defined as the update age, we

¹Due to the fluctuation in the energy arrival process, strictly periodic sensing and transmission is not possible. In this paper, ‘periodic’ is used to indicate that the sensor alternates between sensing and transmission(s) in order to keep status updating at the sink.

²The term update age is inspired by [18] and indicates the age or timeliness of the transmitted information, since an outdated message may lose its value in a communication system when the receiver has interest in fresh information [19]. Note that this notion of the delay is in fact the same as the transmission delay in [13].

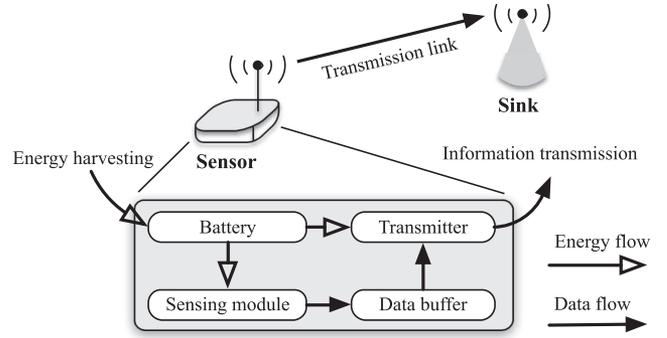


Fig. 1. Illustration of system model and sensor components.

also characterize the frequency of updating the information held by the sink, defined as the update cycle.

- Considering a Rayleigh fading wireless channel, we analytically derive the statistics of both the update cycle and the update age. We consider both a deterministic energy arrival model and a random energy arrival model with a general distribution, so that our results can be applied to model a wide range of EH processes.
- We take the energy costs of both sensing and transmission into account when studying the delay performance. Such a consideration brings up an interesting question of whether to increase or reduce the number of allowed retransmission attempts for each sensed information, because both sensing and transmission consume energy. This in turn results in a tradeoff between the update cycle and the update age. The tradeoff emphasizes the importance of modeling the energy cost of sensing.

Notations: $\mathbb{E}\{\cdot\}$ and $\Pr\{\cdot\}$ are expectation and probability operators, respectively. Convolution operators for continuous and discrete functions are denoted as \star and $*$, respectively. $\lceil \cdot \rceil$ and $\lfloor \cdot \rfloor$ are ceiling and floor operators, respectively. $\sum_{i=m}^n$ is the summation operator, and if $m > n$, the result is zero. $\text{Pois}(i, \lambda)$ is the probability mass function (pmf) of a Poisson distribution with parameter λ .

II. SYSTEM MODEL

We consider the transmission scenario where a sensor periodically transmits its sensed information to a sink, as illustrated in Fig. 1. The sensor is an EH node which harvests energy from the ambient environment such as solar, wind, vibration or RF signals. The sensor has two main functions, i.e., sensing and transmission, each having individual energy cost. We assume half-duplex operation, i.e., sensing and transmission cannot occur at the same time. In order to perform either sensing or transmission, the sensor first needs to spend a certain amount of time on EH. The harvested energy is stored in a battery. We assume that the battery cannot charge and discharge at the same time [16]. In addition, the battery has sufficient charge capacity such that the amount of energy stored in the battery never reaches its maximum capacity. This assumption is reasonable since battery capacity typically ranges from joules

to thousands of joules [1], while the energy level in the battery in our system is only in the μJ range as shown in Section V.

Following state-of-the-art EH sensor design practice [20], we adopt a time-slotted or block-wise operation. We assume that one sensing operation or one transmission is performed in one time block of duration T seconds.³ At the beginning of each block, we assume that the sensor checks the battery energy state and makes a decision to perform either sensing, transmission, or energy harvesting. Thus, we define the following types of time blocks with the associated amount of energy cost/harvesting:

- Sensing Block (SB): the sensor samples the status information and then processes and packs sensed information into a data packet. The energy cost in a SB is denoted by \mathcal{E}_{SB} .
- Transmission Block (TB): the sensor transmits the newest generated data packet (from the last sensing operation) to the sink with energy cost \mathcal{E}_{TB} , i.e., the transmit power is $\mathcal{P}_{\text{TB}} = \mathcal{E}_{\text{TB}}/T$. Then the sink sends a one-bit feedback signal to the sensor to indicate successful packet reception. We assume that the time consumed for receiving the feedback signal at the sensor is negligible as compared to its packet transmission time. If the transmission is successful, we have a successful transmission block (STB); otherwise, we have a failed transmission block (FTB). We assume that successes/failures of each TB are mutually independent [13], [14]. *The probability of a TB being a FTB, i.e., transmission outage, is denoted by P_{out} .*
- Energy-harvesting block (EHB): the sensor harvests energy from the ambient environment and stores the energy in its battery.

A. Proposed Sensing and Transmission Protocol

Since the time-varying EH process results in randomness in the delay for performing sensing and transmission, we propose a harvest-then-use protocol with a time window for retransmissions in order to improve the delay-related performance.

The protocol is motivated as follows. *Firstly*, considering the energy cost of sensing, it is necessary to harvest sufficient energy, \mathcal{E}_{SB} , before sensing can occur. However, it is unwise to perform sensing as soon as the harvested energy reaches \mathcal{E}_{SB} because there will be insufficient energy left for transmission after the sensing operation. The time spent on EH due to insufficient energy for transmitting the sensed information will result in unnecessary delay. To avoid such delay, we define the condition for the sensing operation to be when the harvested energy in the battery exceeds $\mathcal{E}_{\text{SB}} + \mathcal{E}_{\text{TB}}$. In this way, a transmission of sensed information occurs immediately after the sensing operation (i.e., a SB is always followed by a TB). *Secondly*, in the event that the transmission is not successful due to the fading channel between the sensor and sink, we need to allow for retransmissions, which are a common feature in

conventional (non-EH) WSNs [21]. In this paper, we impose a time window for retransmissions to control the delay caused by unsuccessful transmissions because it is unwise to spend an indefinite amount of time trying to transmit outdated information. We denote W as the maximum number of time blocks after a SB, within which transmissions of the currently sensed information can take place. Since the first transmission attempt always happens immediately after the SB, the time window for retransmissions is $W - 1$ time blocks.

Under the proposed protocol, the sensor operates as follows:

- 1) First, the sensor uses several EHBs to harvest enough energy, $\mathcal{E}_{\text{SB}} + \mathcal{E}_{\text{TB}}$, and then a SB and a TB occur.
- 2) If the transmission in the TB is successful, i.e., we have a STB, the sensor harvests energy (taking several EHBs) for the next sensing period until the battery energy exceeds $\mathcal{E}_{\text{SB}} + \mathcal{E}_{\text{TB}}$.
- 3) If the transmission in the TB fails, i.e., we have a FTB, the sensor goes back to harvesting energy (taking several EHBs) and performs a retransmission when the battery energy exceeds \mathcal{E}_{TB} .
- 4) Retransmission may occur several times until the sensed information is successfully transmitted to the sink or the time window for retransmissions $W - 1$ is reached. Then, the data packet at the sensor is dropped and the sensor goes back to harvesting the energy for a new sensing operation.

Fig. 2 illustrates this protocol with $W = 7$. In the example shown, the first block in Fig. 2 is a SB, followed by two FTBs (and two EHBs in between). Since the third TB is a STB, the sensed information in the first SB is successfully transmitted to the sink. Then, the sensor uses three EHBs to harvest energy to conduct sensing in the next SB. After the second SB, there are three TBs during 7 time blocks, and all of them are FTBs. Thus, the retransmission process is terminated after $W = 7$ is reached. As a result, the sensed information in the second SB is not transmitted to the sink. The time indices shown in Fig. 2 will be defined in the following section.

B. Proposed Models for Energy Arrival

In this paper, we consider that the harvested energy in each EHB could either *remain constant* or *change* from block to block. The former is referred to as deterministic energy arrival, while the latter is referred to as random energy arrival.

Deterministic energy arrival is an appropriate model when the coherence time of the EH process is much larger than the duration of the entire communication session, such as EH by solar panel on clear days [12], [22], [23]. In this paper, we denote this as *deterministic energy arrival process*. For tractability, we also assume that \mathcal{E}_{SB} and \mathcal{E}_{TB} represent integer multiples of the harvested energy by one EHB, ρ .

For random energy arrivals, we consider independent and identically distributed (i.i.d.) random energy arrival model⁴

³In general a sensor may spend different amounts of time on one sensing operation [10]. Thus, the assumed protocol and analysis can be generalized to different sensing time durations other than T , which is outside the scope of this work.

⁴The i.i.d. energy arrival model is commonly considered in the literature [16], [24], [25]. There are other energy arrival models captures the temporal correlation of the energy arrival process, such as discrete-Markovian modeling [8], [9], [26], which are beyond the scope of this work.

the available energy after $t_{\text{STB},j}$ is the same for all j . Because the successes/failures of each TB are mutually independent, and $T_{\text{UC},j}$ is determined by both the available energy after $t_{\text{STB},j}$ and the successes/failures of the following TBs, $T_{\text{UC},j}$ are i.i.d. for all j . Similarly, it is also easy to show that $T_{\text{UA},j}$ are i.i.d. for all j . For convenience, we remove subscript j for T_{UC} and T_{UA} in (2) and (1), respectively.

IV. UPDATE AGE

In this section, considering the dynamics of an energy arrival process and the probability of successful/failed transmission in our proposed harvest-then-use protocol, the update age for deterministic, general random and exponential energy arrival processes are analyzed.

A. Deterministic Energy Arrival Process

Theorem 1: For a deterministic energy arrival process, the update age pmf is given by

$$\Pr\{T_{\text{UA}} = k\} = \frac{(1 - P_{\text{out}})(P_{\text{out}})^{n-1}}{P_{\text{suc}}},$$

$$k = 1 + (n-1) \left(\frac{\mathcal{E}_{\text{TB}}}{\rho} + 1 \right), \quad (4)$$

where

$$n = 1, 2, \dots, \hat{n}, \quad \hat{n} = 1 + \left\lfloor \frac{W-1}{1 + \frac{\mathcal{E}_{\text{TB}}}{\rho}} \right\rfloor, \quad P_{\text{suc}} = 1 - (P_{\text{out}})^{\hat{n}}, \quad (5)$$

and P_{out} is the probability of a TB being a FTB, defined in Section II.

Proof: See Appendix D. ■

From Theorem 1, the average update age, \bar{T}_{UA} for a deterministic energy arrival process is straightforwardly obtained as in Corollary 1.

Corollary 1: For a deterministic energy arrival process, average update age is given by

$$\bar{T}_{\text{UA}} = \sum_{n=1}^{\hat{n}} \left(1 + (n-1) \left(\frac{\mathcal{E}_{\text{TB}}}{\rho} + 1 \right) \right) \frac{(1 - P_{\text{out}})(P_{\text{out}})^{n-1}}{P_{\text{suc}}}, \quad (6)$$

where P_{suc} is given in (5).

B. General Random Energy Arrival Process

Theorem 2: For a general random energy arrival process, the update age pmf⁵ is given by

$$\Pr\{T_{\text{UA}}=k\} = \begin{cases} \frac{1 - P_{\text{out}}}{P_{\text{suc}}}, & k = 1, \\ \frac{(1 - P_{\text{out}})}{P_{\text{suc}}} \sum_{n=2}^k (P_{\text{out}})^{n-1} (G_{k-n-1}((n-1)\mathcal{E}_{\text{TB}}) - G_{k-n}((n-1)\mathcal{E}_{\text{TB}})), & 2 \leq k \leq W, \end{cases} \quad (7)$$

⁵Although the general expression in Theorem 2 contains multiple integrals in Eq. (9), for special cases, such as deterministic and exponential energy arrival processes, the results given in Theorems 1 and 3 are closed-form expressions.

where

$$P_{\text{suc}} = 1 - P_{\text{out}} + (1 - P_{\text{out}}) \sum_{l=2}^W \sum_{n=2}^l (P_{\text{out}})^{n-1} \times (G_{l-n-1}((n-1)\mathcal{E}_{\text{TB}}) - G_{l-n}((n-1)\mathcal{E}_{\text{TB}})), \quad (8)$$

and

$$G_i(x) = \begin{cases} 1, & i = -1, \\ \int_0^x \underbrace{(g \star f \star f \star \dots \star f)}_{i \text{ convolutions}}(u) du, & i \geq 0. \end{cases} \quad (9)$$

$g(x)$ and $f(x)$ are defined in Lemma 1.

Proof: See Appendix D. ■

From Theorem 2, the average update age, \bar{T}_{UA} for a general random energy arrival process is obtained straightforwardly as in Corollary 2.

Corollary 2: For a general random energy arrival process, average update age is given by

$$\bar{T}_{\text{UA}} = \frac{1 - P_{\text{out}}}{P_{\text{suc}}} \left(1 + \sum_{l=2}^W l \sum_{n=2}^l (P_{\text{out}})^{n-1} (G_{l-n-1}((n-1)\mathcal{E}_{\text{TB}}) - G_{l-n}((n-1)\mathcal{E}_{\text{TB}})) \right), \quad (10)$$

where P_{suc} is given in (8).

C. Exponential Energy Arrival Process

Theorem 3: For an exponential energy arrival process, the update age pmf is given by

$$\Pr\{T_{\text{UA}} = k\} = \begin{cases} \frac{1 - P_{\text{out}}}{P_{\text{suc}}}, & k = 1, \\ \frac{(1 - P_{\text{out}})}{P_{\text{suc}}} \sum_{n=2}^k (P_{\text{out}})^{n-1} \times \text{Pois} \left(k - n, (n-1) \frac{\mathcal{E}_{\text{TB}}}{\rho} \right), & 2 \leq k \leq W, \end{cases} \quad (11)$$

where

$$P_{\text{suc}} = 1 - P_{\text{out}} + (1 - P_{\text{out}}) \sum_{l=2}^W \sum_{n=2}^l (P_{\text{out}})^{n-1} \text{Pois} \left(l - n, (n-1) \frac{\mathcal{E}_{\text{TB}}}{\rho} \right), \quad (12)$$

Proof: See Appendix D. ■

From Theorem 3, the average update age, \bar{T}_{UA} for an exponential energy arrival process is straightforwardly obtained as in Corollary 3.

Corollary 3: For an exponential energy arrival process, average update age is given by

$$\bar{T}_{\text{UA}} = \frac{(1 - P_{\text{out}})}{P_{\text{suc}}} \left(1 + \sum_{l=2}^W l \sum_{n=2}^l (P_{\text{out}})^{n-1} \text{Pois} \left(l - n, (n-1) \frac{\mathcal{E}_{\text{TB}}}{\rho} \right) \right), \quad (13)$$

where P_{suc} is given in (12).

From Theorems 1–3 and Corollaries 1–3, we see that different energy arrival processes induce different pmfs and average values of update age. For benchmarking with the existing studies on delay without imposing a constraint on the time window for retransmissions [13], we let $W \rightarrow \infty$, so that all sensed information is eventually transmitted to the sink, the average update age is the same under different energy arrival processes as in Corollary 4.

Corollary 4: For a deterministic or general random energy arrival process, \bar{T}_{UA} increases with W , and as W gets large, the asymptotic upper bound of \bar{T}_{UA} is independent of energy arrival distribution and is given by

$$\lim_{W \rightarrow \infty} \bar{T}_{\text{UA}} = 1 + \frac{P_{\text{out}}}{1 - P_{\text{out}}} \left(\frac{\mathcal{E}_{\text{TB}}}{\rho} + 1 \right). \quad (14)$$

Proof: See Appendix G. ■

Remark 3: From the above analytical results, we have that:

- i) From Theorems 1 to 3, T_{UA} is independent of the energy cost of sensing, \mathcal{E}_{SB} , because the delay is only affected by the energy harvesting and retransmissions that happen after the sensing operation. This might give the impression that energy cost of sensing does not affect delay. However, update age is only one of the two delay metrics, and the energy cost of sensing has important impacts on update cycle, which will be investigated in the next section.
- ii) Allowing a larger window for retransmissions increases the average update age. This might suggest that retransmissions should be avoided, i.e., $W = 1$. However, the update age does not take into account cases where sensed information is not successfully transmitted to the sink. In this regard, the update cycle implicitly captures such cases.

V. UPDATE CYCLE

In this section, considering the dynamics of an energy arrival process and the probability of successful/failed transmission in our proposed harvest-then-use protocol, the update cycle for deterministic, general random and exponential energy arrival processes are analyzed.

A. Deterministic Energy Arrival Process

Theorem 4: For a deterministic energy arrival process, the update cycle pmf is given by

$$\Pr \{T_{\text{UC}} = k\} = (1 - P_{\text{out}}) (P_{\text{out}})^{n-1+m\hat{n}},$$

$$k = \left(\frac{\mathcal{E}_{\text{SB}} + n\mathcal{E}_{\text{TB}}}{\rho} \right) + n + 1 + m \left(\frac{\mathcal{E}_{\text{SB}} + \hat{n}\mathcal{E}_{\text{TB}}}{\rho} + (\hat{n} + 1) \right), \quad (15)$$

where $n = 1, 2, \dots, \hat{n}$, $m = 0, 1, 2, \dots$, and \hat{n} is given in (5).

Proof: See Appendix E. ■

Corollary 5: For a deterministic energy arrival process, average of update cycle is given by

$$\bar{T}_{\text{UC}} = \frac{(P_{\text{out}})^{\hat{n}}}{1 - (P_{\text{out}})^{\hat{n}}} \left(1 + \hat{n} + \frac{\mathcal{E}_{\text{SB}} + \hat{n}\mathcal{E}_{\text{TB}}}{\rho} \right) + \frac{\mathcal{E}_{\text{SB}}}{\rho} + 1$$

$$+ \left(1 + \frac{\mathcal{E}_{\text{TB}}}{\rho} \right) \frac{1 - P_{\text{out}}}{1 - (P_{\text{out}})^{\hat{n}}} \sum_{n=1}^{\hat{n}} (P_{\text{out}})^{n-1} n. \quad (16)$$

Proof: See Appendix F. ■

B. General Random Energy Arrival Process

Theorem 5: For a general random energy arrival process, the update cycle pmf is given by

$$\Pr \{T_{\text{UC}} = k\} = \sum_{m=0}^{\hat{m}} \left(\zeta(\mathcal{E}_{\text{SB}} + \mathcal{E}_{\text{TB}}) \underbrace{* \zeta(\mathcal{E}_{\text{SB}}) * \dots * \zeta(\mathcal{E}_{\text{SB}})}_{m \text{ convolutions}} \right.$$

$$\left. * \underbrace{\vartheta * \dots * \vartheta * \iota}_{m \text{ convolutions}} \right) (k - m(1 + W) - 1), k = 2, 3, \dots \quad (17)$$

where $\hat{m} = \lfloor \frac{k-2}{W+1} \rfloor$, and functions $\zeta(\mathcal{E}, i)$, $\iota(i)$ and $\vartheta(i)$ are given by

$$\zeta(\mathcal{E}, i) = G_{i-1}(\mathcal{E}) - G_i(\mathcal{E}), \quad (18a)$$

$$\iota(i) = P_{\text{suc}} \Pr \{T_{\text{UA}} = i\}, \quad (18b)$$

$$\vartheta(i) = P_{\text{out}} (G_{W+i-2}(\mathcal{E}_{\text{TB}}) - G_{W+i-1}(\mathcal{E}_{\text{TB}}))$$

$$+ \sum_{l=2}^W \sum_{n=2}^l (P_{\text{out}})^n (G_{l-n-1}((n-1)\mathcal{E}_{\text{TB}}) - G_{l-n}((n-1)\mathcal{E}_{\text{TB}}))$$

$$\times (G_{W+i-l-1}(\mathcal{E}_{\text{TB}}) - G_{W+i-l}(\mathcal{E}_{\text{TB}})). \quad (18c)$$

$\Pr \{T_{\text{UA}} = i\}$, P_{suc} and $G_i(\mathcal{E})$ are given in (7), (8) and (9), respectively.

Proof: See Appendix E. ■

Corollary 6: For a general random energy arrival process, average update cycle is given by

$$\bar{T}_{\text{UC}} = \frac{1 - P_{\text{suc}}}{P_{\text{suc}}} \left(\frac{\mathcal{E}_{\text{SB}}}{\rho} + \bar{V} + W + 1 \right)$$

$$+ \frac{\mathcal{E}_{\text{SB}} + \mathcal{E}_{\text{TB}}}{\rho} + \bar{T}_{\text{UA}} + 1, \quad (19)$$

where P_{suc} and \bar{T}_{UA} are respectively given in (8) and (10), and \bar{V} is given in (20) shown at the bottom of the next page.

Proof: See Appendix F. ■

C. Exponential Energy Arrival Process

Theorem 6: For an exponential energy arrival process, the update cycle pmf is given by

$$\Pr \{T_{UC} = k\} = \sum_{m=0}^{\hat{m}} \left(\underbrace{\zeta((m+1)\mathcal{E}_{SB} + \mathcal{E}_{TB})}_{m \text{ convolutions}} * \vartheta * \dots * \vartheta * \iota \right) (k - m(1+W) - 1), k = 2, 3, \dots \quad (21)$$

where $\hat{m} = \lfloor \frac{k-2}{W+1} \rfloor$, and functions $\zeta(\mathcal{E}, i)$, $\iota(i)$ and $\vartheta(i)$ are given by

$$\zeta(\mathcal{E}, i) = \text{Pois}(i, \mathcal{E}/\rho), \quad (22a)$$

$$\iota(i) = P_{\text{suc}} \Pr \{T_{UA} = i\}, \quad (22b)$$

$$\begin{aligned} \vartheta(i) = & P_{\text{out}} \text{Pois}(W+i-1, \mathcal{E}_{TB}/\rho) \\ & + \sum_{l=2}^W \sum_{n=2}^l (P_{\text{out}})^n \text{Pois}(l-n, (n-1)\mathcal{E}_{TB}/\rho) \times \\ & \text{Pois}(W+i-l, \mathcal{E}_{TB}/\rho), \end{aligned} \quad (22c)$$

and $\Pr \{T_{UA} = i\}$ and P_{suc} are given in (11) and (12), respectively.

Proof: See Appendix E. \blacksquare

Corollary 7: For an exponential energy arrival process, average update cycle is given by

$$\bar{T}_{UC} = \frac{1 - P_{\text{suc}}}{P_{\text{suc}}} \left(\frac{\mathcal{E}_{SB}}{\rho} + \bar{V} + W + 1 \right) + \frac{\mathcal{E}_{SB} + \mathcal{E}_{TB}}{\rho} + \bar{T}_{UA} + 1, \quad (23)$$

where \bar{T}_{UA} and P_{suc} are given in (13) and (12), and \bar{V} is given in (24) shown at the bottom of the page.

Proof: See Appendix F. \blacksquare

Similar with the case of update age, different energy arrival processes induces different pmfs and average values of update

cycle. However, for benchmarking with the existing studies on delay without imposing a constraint on the maximum allowable retransmission time, when we consider removing the constraint of retransmission, i.e., $W \rightarrow \infty$, so that all sensed information is eventually transmitted to the sink, the average update cycle is the same under different energy arrival processes as in Corollary 8.

Corollary 8: For a deterministic or general random energy arrival process, \bar{T}_{UC} decreases with W , and as W grows large, the asymptotic lower bound of \bar{T}_{UC} is independent with energy arrival distribution and is given by

$$\lim_{W \rightarrow \infty} \bar{T}_{UC} = 2 + \frac{\mathcal{E}_{SB} + \mathcal{E}_{TB}}{\rho} + \frac{P_{\text{out}}}{1 - P_{\text{out}}} \left(\frac{\mathcal{E}_{TB}}{\rho} + 1 \right). \quad (25)$$

Proof: See Appendix G. \blacksquare

Remark 4: From the above analytical results, we have that:

- i) From Theorems 4 to 6, we know that T_{UC} is affected by the energy cost of sensing, \mathcal{E}_{SB} . A larger \mathcal{E}_{SB} means more EHBs are required to harvest a sufficient amount of energy to perform sensing operation(s) between adjacent STBs.
- ii) A larger window for retransmissions shorten the average update cycle, because allowing more retransmissions increases the chance of having a successful transmission. This might suggest that it is also better to increase W to reduce the update cycle. But increasing W also increases the update age as discussed earlier. Therefore, there is clearly a tradeoff between the two metrics.

VI. NUMERICAL RESULTS

In this section, we present numerical results for the update age and update cycle, using the results in Theorems 1-6 and Corollaries 1-8. The typical outdoor range for a wireless sensor is from 75 m to 100 m [27]. Hence, we set the distance between the sensor and the sink as $d = 90$ m and the path loss exponent

$$\begin{aligned} \bar{V} = & \frac{P_{\text{out}}}{1 - P_{\text{suc}}} \left(\frac{\mathcal{E}_{TB}}{\rho} - \sum_{i=0}^{W-2} i (G_{i-1}(\mathcal{E}_{TB}) - G_i(\mathcal{E}_{TB})) - (W-1) \left(1 - \sum_{i=0}^{W-2} (G_{i-1}(\mathcal{E}_{TB}) - G_i(\mathcal{E}_{TB})) \right) \right) \\ & + \frac{1}{1 - P_{\text{suc}}} \sum_{l=2}^W \sum_{n=2}^l (P_{\text{out}})^n (G_{l-n-1}((n-1)\mathcal{E}_{TB}) - G_{l-n}((n-1)\mathcal{E}_{TB})) \\ & \times \left(\frac{\mathcal{E}_{TB}}{\rho} - \sum_{i=0}^{W-l-1} i (G_{i-1}(\mathcal{E}_{TB}) - G_i(\mathcal{E}_{TB})) - (W-l) \left(1 - \sum_{i=0}^{W-l-1} (G_{i-1}(\mathcal{E}_{TB}) - G_i(\mathcal{E}_{TB})) \right) \right) \end{aligned} \quad (20)$$

$$\begin{aligned} \bar{V} = & \frac{P_{\text{out}}}{1 - P_{\text{suc}}} \left(\frac{\mathcal{E}_{TB}}{\rho} - \sum_{i=0}^{W-2} i \text{Pois} \left(i, \frac{\mathcal{E}_{TB}}{\rho} \right) - (W-1) \left(1 - \sum_{i=0}^{W-2} \text{Pois} \left(i, \frac{\mathcal{E}_{TB}}{\rho} \right) \right) \right) + \frac{1}{1 - P_{\text{suc}}} \\ & \times \sum_{l=2}^W \sum_{n=2}^l (P_{\text{out}})^n \text{Pois} \left(l-n, (n-1) \frac{\mathcal{E}_{TB}}{\rho} \right) \left(\frac{\mathcal{E}_{TB}}{\rho} - \sum_{i=0}^{W-l-1} i \text{Pois} \left(i, \frac{\mathcal{E}_{TB}}{\rho} \right) - (W-l) \left(1 - \sum_{i=0}^{W-l-1} \text{Pois} \left(i, \frac{\mathcal{E}_{TB}}{\rho} \right) \right) \right) \end{aligned} \quad (24)$$

for the sensor-sink transmission link as $\lambda = 3$ [13]. The duration of a time block is $T = 5$ ms [22]. The noise power at the sink is $\sigma^2 = -100$ dBm [14]. The average harvested power is 10 mW [28], i.e., average harvested energy per time block, $\rho = 50 \mu\text{J}$. Unless otherwise stated, (i) we set the power consumption in each TB, $\mathcal{P}_{\text{TB}} = 40$ mW, i.e., $\mathcal{E}_{\text{TB}} = 200 \mu\text{J}$. Note that this includes RF circuit consumption (main consumption) and the actual RF transmit power $\mathcal{P}_{\text{tx}} = -5$ dBm⁶ and (ii) we set the power consumption in each SB as $\mathcal{P}_{\text{SB}} = 50$ mW [10], i.e., $\mathcal{E}_{\text{SB}} = 250 \mu\text{J}$. In the following calculations, power and SNR related quantities use a linear scale. We assume that a transmission outage from the sensor to the sink occurs when the SNR at the sink γ , is lower than SNR threshold $\gamma_0 = 40$ dB [15]. The outage probability is

$$P_{\text{out}} = \Pr \{ \gamma < \gamma_0 \}. \quad (26)$$

The SNR at the sink is [29]

$$\gamma = \frac{|h|^2 \mathcal{P}_{\text{tx}}}{\Gamma d^\lambda \sigma^2}, \quad (27)$$

where h is the source-sink channel fading gain, $\Gamma = \frac{P_L(d_0)}{d_0^\lambda}$, is a path loss factor relative to reference distance d_0 of the antenna far field, and $P_L(d_0)$ is linear-scale path loss, which depends on the propagation environment [13]. Following [13], [14], we assume $\Gamma = 1$, for simplicity.

For the numerical results, we assume that h is block-wise Rayleigh fading. Using (27), the outage probability can be written as

$$P_{\text{out}} = 1 - \exp\left(-\frac{d^\lambda \sigma^2 \gamma_0}{\mathcal{P}_{\text{tx}}}\right). \quad (28)$$

By applying (28) to the theorems and corollaries in Sections IV and V, we compute the expressions of the pmfs of T_{UA} and T_{UC} as well as their average values \bar{T}_{UA} and \bar{T}_{UC} .

Pmfs of update age and update cycle with different energy arrival processes: First, we consider a deterministic energy arrival process with harvested energy in each EHB, ρ . Also we consider two special cases of the general random energy arrival process: (i) exponential energy arrival processes with average harvested energy in each EHB, ρ and (ii) random energy arrival processes with gamma distribution [16], Gamma(0.05, 1000). We term this as the *gamma energy arrival process*, and it is easy to verify that this gamma energy arrival process has the same average harvested energy in each EHB as the deterministic and exponential energy arrival processes.

Figs. 3–5 plot the pmfs of update age, T_{UA} , and update cycle, T_{UC} , for the deterministic, gamma and exponential energy arrival process, respectively. The analytical results are plotted using Theorems 1–6, and we set $W = 50$, i.e., the time window for retransmissions is $W - 1 = 49$ time blocks. In particular, in Fig. 4 the analytical pmfs of T_{UA} and T_{UC} for the general random arrival process are obtained using Theorems 2 and 5. The results in Figs. 4–5 also illustrate the importance of the

⁶The values we chose for \mathcal{P}_{TB} and \mathcal{P}_{tx} are typical for commercial sensor platforms, such as MICAz [27].

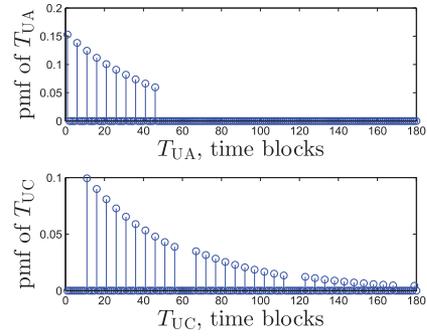


Fig. 3. pmfs for T_{UA} and T_{UC} with deterministic energy arrival process.

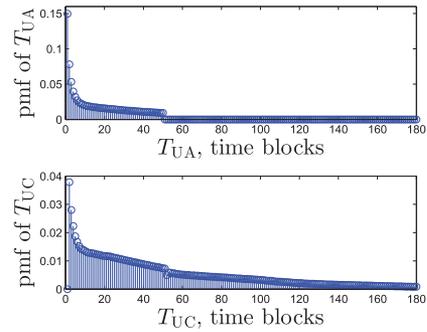


Fig. 4. pmfs for T_{UA} and T_{UC} with gamma energy arrival process.

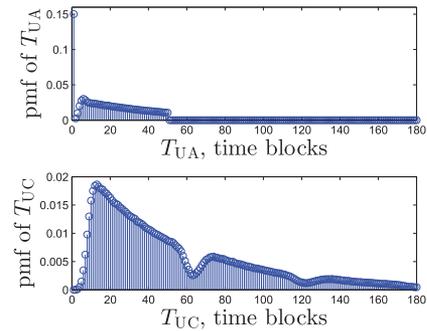


Fig. 5. pmfs for T_{UA} and T_{UC} with exponential energy arrival process.

general random energy arrival process, which is used in this work. This is because gamma and exponential energy arrival processes, which have been used in the literature [13]–[16], are special cases of the general random energy arrival process. *We see that different energy arrival processes result in different pmfs of update age and update cycle. Hence, a statistical analysis of the two metrics will provide insight into the design of future EH WSNs.*

In the following figures (Figs. 6–9), we only present the numerical results for the average values of the two delay metrics, which have been presented in Corollaries 1–8.

Average update age and average update cycle with different energy arrival processes: Figs. 6 and 7 show the average update age, \bar{T}_{UA} , and the average update cycle, \bar{T}_{UC} , for different W , i.e., different time windows for retransmissions, $W - 1$, and energy arrival processes. The results in Figs. 6 and 7 are generated using Corollaries 1–4 and Corollaries 5–8, respectively. We can see that the different energy arrival models

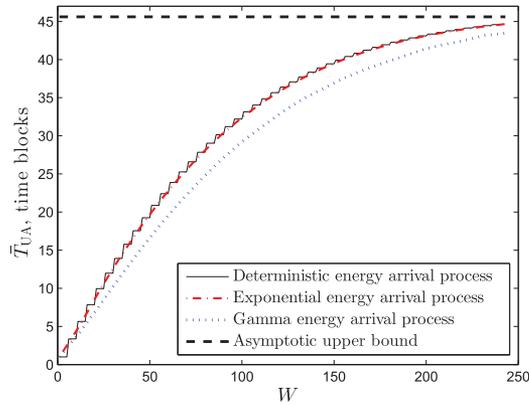


Fig. 6. Average update age, \bar{T}_{UA} , versus W , with different energy arrival processes.

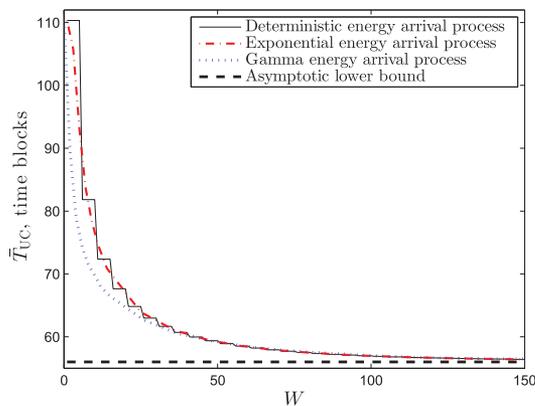


Fig. 7. Average update cycle, \bar{T}_{UC} , versus W , with different energy arrival processes.

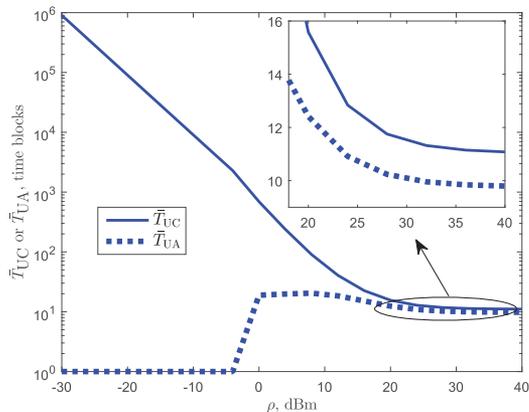


Fig. 8. \bar{T}_{UC} and \bar{T}_{UA} versus ρ with exponential energy arrival process.

result in almost the same values of the average update age and especially the average update cycle. As the time window for retransmissions increases, the average update age increases monotonically and approaches its analytical upper bound given by Corollary 4, while the average update cycle decreases monotonically and approaches its analytical lower bound given by Corollary 8. Thus, with a smaller time window for retransmissions, the updated status is more fresh, but the update frequency is lower.

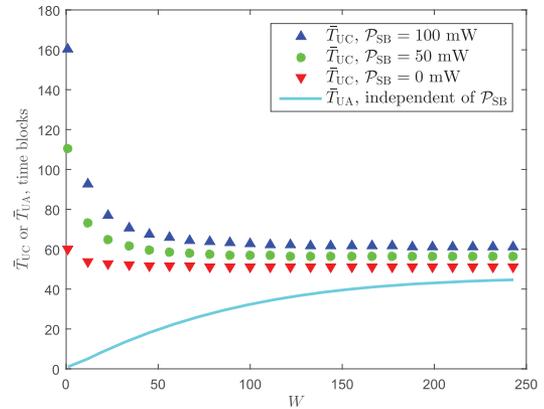


Fig. 9. \bar{T}_{UC} and \bar{T}_{UA} versus W for different sensing power, \mathcal{P}_{SB} .

Average update age and average update cycle with different average harvested power: Fig. 8 shows the average update age, \bar{T}_{UA} , and the average update cycle, \bar{T}_{UC} , for different average harvested power values, ρ , with an exponential energy arrival process. The results are plotted using Corollaries 3 and 7. For the update age, we see that when the average harvested power is very low, i.e., less than -2 dBm, the update age is one time block. This is expected since sufficiently low average harvested power cannot enable any retransmission during time window $W - 1$, i.e., a packet is either successfully transmitted in the first transmission block right after the sensing block (an update age of one) or dropped due to no chance of retransmission. With an increase of average harvested power, retransmissions are enabled, which makes the update age increases beyond one. However, when the average harvested power is higher than 8 dBm, the average update age monotonically decreases with an increase of the average harvested power. This is as expected: the sensor requires fewer energy harvesting blocks to perform retransmissions, and hence, the sink is likely to receive the packet in a more timely manner (i.e., with a smaller update age). For the update cycle, we see that the average update cycle monotonically decreases with average harvested power. Again, this is expected since a higher average harvested power enables more transmission blocks within a certain time duration, and hence, more successful block transmissions are likely to occur within a given time duration, i.e., the update cycle decreases. Also we see that when the average harvested power is very high, i.e., $\rho \geq 30$ dBm, both update age and update cycle converge to constant values which can be obtained by letting $\rho \rightarrow \infty$ in Corollaries 3 and 7, respectively. Thus, without changing the parameters of the communication protocol, the improvement in delay performance is limited when increasing the average harvested power.

Effect of energy cost of sensing on average update cycle: We illustrate the effect of energy cost of sensing on average update cycle with exponential energy arrival process as a special case of the random energy arrival process. Fig. 9 shows the average update age, \bar{T}_{UA} , and the average update cycle, \bar{T}_{UC} , as a function of W , with different energy cost of sensing, \mathcal{P}_{SB} . The figure shows that the average update age increases as W increases (consistent with Fig. 6 but it does not change with the energy cost of sensing, i.e., the energy cost of sensing has

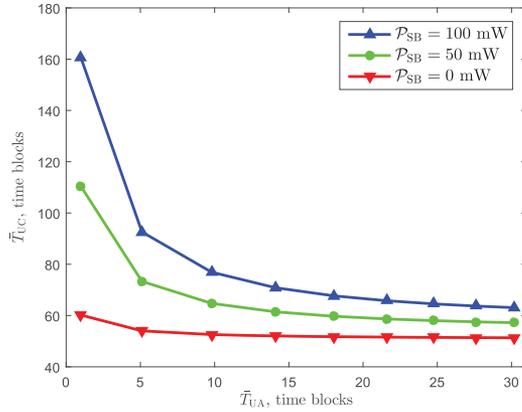


Fig. 10. Tradeoff between \bar{T}_{UC} and \bar{T}_{UA} .

no effect on the update age. This is in perfect agreement with our earlier observations and explanations provided in Remark 3. We can see that for a fixed value of W , the average update cycle increases as the sensing power consumption increases from 50 mW to 100 mW, i.e., *the higher the energy cost of sensing the lower update frequency*. This is in perfect agreement with our earlier observations and explanations provided in Remark 4. To place these results in context with existing studies in the literature that commonly ignore the energy cost of sensing, we also include the result with zero energy cost of sensing. When $\mathcal{P}_{SB} = 0$ mW, we can see that \bar{T}_{UC} is almost constant around the value of 50 and does not vary much with W .

Tradeoff between average update age and average update cycle: Fig. 10 shows the tradeoff between average update age, \bar{T}_{UA} , and average update cycle, \bar{T}_{UC} with exponential energy arrival process. The different points on the same curve are achieved with different W . We can see that when the energy cost of sensing is comparable to or larger than the energy cost of transmission, e.g., $\mathcal{P}_{SB} = 50$ mW and $\mathcal{P}_{SB} = 100$ mW, the reduction in \bar{T}_{UA} can result in a significant increase in \bar{T}_{UC} , and vice versa. For example, when $\mathcal{P}_{SB} = 100$ mW, decreasing \bar{T}_{UA} from 15 to 5 time blocks, causes the \bar{T}_{UC} to increase from 75 to 95 time blocks. However, when the sensing is negligible, e.g., $\mathcal{P}_{SB} = 0$ mW, such a tradeoff is almost barely noticeable. For example, decreasing \bar{T}_{UA} from 15 to 5 time blocks, results in \bar{T}_{UC} increasing by two time blocks, i.e., a significant change in \bar{T}_{UA} does not result in a noticeable change in \bar{T}_{UC} . These trends in Fig. 10 are in accordance with our earlier observations in Remark 4. *Thus, with the consideration of sensing energy cost, an increase of update frequency is achieved at the expense of update freshness, and vice versa.*

Effect of transmit power consumption on average update age and average update cycle. Fig. 11 shows the impact of power consumption on \bar{T}_{UA} and \bar{T}_{UC} , for different values of transmit power \mathcal{P}_{TB} and RF transmit power \mathcal{P}_{TX} , with an exponential energy arrival process. In reality, \mathcal{P}_{TB} and \mathcal{P}_{TX} do not have a linear relationship. Three pairs of typical values found in [25] are chosen. We see that both \bar{T}_{UA} and \bar{T}_{UC} decrease with \mathcal{P}_{TB} or \mathcal{P}_{TX} . This is as expected: if the transmit power is small, P_{out} is high, resulting in a large number of retransmissions until the sensed information is successfully transmitted or $W - 1$ time blocks are reached. As a result, \bar{T}_{UA} and \bar{T}_{UC} are large

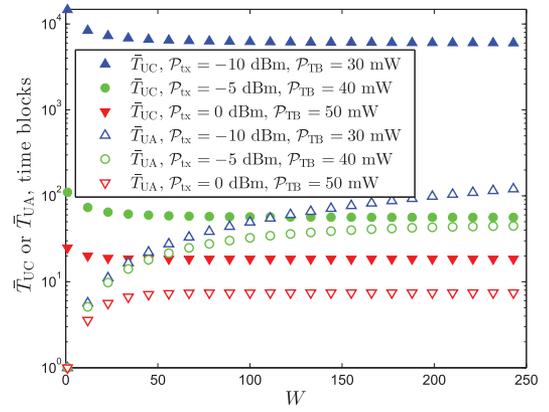


Fig. 11. \bar{T}_{UC} and \bar{T}_{UA} versus W with different \mathcal{P}_{TX} and \mathcal{P}_{TB} .

when the transmit power is small. *Thus, under these above parameter choices, a higher transmit power results in better delay performance.*

VII. CONCLUSIONS

This paper has analysed the delay performance of an EH sensor network, focusing on the operation of a single EH sensor and its information transmission to a sink. The energy costs of both sensing and transmission were taken into account. Two metrics were proposed, namely the update age and update cycle. In order to limit the delay due to retransmissions, a time window for retransmissions was imposed. Using both a deterministic and a general random energy arrival model, the exact probability mass functions and the mean values of both metrics were derived. The results showed that the average update age increases while the average update cycle decreases with increasing retransmission window length. The average update age is independent of the energy cost of sensing but the average update cycle increases as the energy cost of sensing increases. In addition, a tradeoff between update age and update cycle was illustrated when the energy cost of sensing is comparable to the energy cost of transmission. Future work can consider the impact of non-deterministic time for receiving the feedback signal at the sensor.

APPENDIX A PROOF OF LEMMA A1

We first define the block-wise harvest-then-use process, and then propose and prove Lemma A1.

Definition A1 (Block-wise harvest-then-use process): A harvest-then-use process consists of energy harvesting blocks (EHBs) and energy consumption blocks (ECBs). It starts and keeps on harvesting energy with EHBs. Once the available, i.e., accumulated, energy is no less than a threshold of Q Joules, an ECB occurs, and consumes Q Joules of energy. If this condition for ECB is not satisfied, the process goes back to harvest energy with EHBs.

During the harvest-then-use process, the harvested energy in the i th EHB is represented by ξ_i , $i = 1, 2, 3, \dots$, and the available energy after the j th ECB is represented by $\tilde{\xi}_j$, $j = 1, 2, 3, \dots$. Due to the randomness of the energy arrival process, i.e., ξ_i is a random variable, the available energy after

each ECB, $\tilde{\xi}_j$, is also a random variable which only depends on ξ_i . Furthermore, using the statistics of ξ_i , and modeling $\tilde{\xi}_j$, $j = 1, 2, 3, \dots$, as a random process, an important feature of the random process is revealed in Lemma A1.

Lemma A1: For block-wise harvest-then-use process with energy threshold Q , where the harvested energy in each EHB, ξ_i , $i = 1, 2, 3, \dots$, are independent and identically distributed, each with pdf containing at least one positive right-continuous point, $f(x)$, the available energy after each ECB, $\tilde{\xi}_j$, $j = 1, 2, 3, \dots$, consists of a positive recurrent Harris chain, with unique steady-state distribution which is given by

$$g(x) = \frac{1}{\rho} (1 - F(x)), \quad (\text{A.1})$$

where $F(x)$ and ρ are respectively, the cdf and the mean of ξ_i .

Proof: The proof consists of two steps. In the first step, we prove that the energy state after the j th ECB, $\tilde{\xi}_j$, constitutes a positive recurrent Harris chain (a collection of Markov chains with uncountable state space). Thus, a unique steady-state distribution of $\tilde{\xi}_j$ exists [30]. In the second step, we prove that (A.1) is the unique steady-state distribution.

Step 1: It is easy to see that the current state, $\tilde{\xi}_j$ takes its value from a continuous state space and only relies on the previous energy state $\tilde{\xi}_{j-1}$, thus $\tilde{\xi}_j$, $j = 1, 2, 3, \dots$, forms a continuous-state Markov chain. Without loss of generality, we assume that $\sup\{\xi_i\} = B$, thus $\sup\{\tilde{\xi}_j\} \leq B$ holds in this harvest-then-use process.⁷ It is easy to see that the state space of Markov chain $\tilde{\xi}_j$, \mathcal{S} , is a subset of $[0, B)$, and because of the harvest-then-use protocol, any current state which is higher than Q , will access the interval $[0, Q)$ in the following steps. Thus, we only need to prove that any state $s \in [0, \min\{B, Q\})$ can hit any arbitrary small interval $\tau = (\tau^-, \tau^+)$ in \mathcal{S} with non-zero probability within finite steps. Actually, in the following, we complete the proof with the assumption that $\mathcal{S} = [0, B)$, which also proves that the state space of Markov chain $\tilde{\xi}_i$ is exactly $[0, B)$.

In the following, using a constructive method, we show that for Markov chain $\tilde{\xi}_j$, given any current state $s \in [0, \min\{B, Q\})$, there is at least a probability, $q \times p$, that any arbitrary small interval τ will be accessed with \tilde{j} steps, where p, q, \tilde{j} are defined below which only depends on the state s , the interval length τ and the pdf of the harvested energy in each EHB.

Since pdf function $f(x)$ has positive right-continuous points on $[0, B)$, there exists at least one interval $[D^-, D)$ that satisfies $[D^-, D) \subset [0, B)$, $D - D^- = \tau/2$, and $f(x)$ is positive right-continuous on $[D^-, D)$. We assume that $D^- \geq \tau^+$, and the $D^- < \tau^+$ case can be easily generated from the following discussions, thus is omitted due to space limitation. Now we define $p \triangleq \int_{D^-}^D f(x)dx$ as the probability that harvested energy in one EHB lies in the interval $[D^-, D)$. Also we define $\tilde{f}(x) = f(x)$ when $x \in [D^-, D)$, otherwise $\tilde{f}(x) = 0$, and $\tilde{f}_i(x)$ is the i -fold convolution of function $\tilde{f}(x)$.

Thus, it is easy to see that $\tilde{f}_i(x)$ is positive and continuous in the interval (iD^-, iD) , and $\int_a^b \tilde{f}_i(x)dx$ is the

⁷Note that although we assume B is finite, the infinite case can be easily generated from the discussions below, thus is omitted due to space limitation.

probability that the harvested energy by i EHBs lies in the interval $[a, b)$, while the energy harvested by each of the i EHBs lies in the interval $[D^-, D)$. Thus, letting $\tilde{i} \triangleq \lceil 4(Q + \tau)/\tau - 1 \rceil$ and $\tilde{j} \triangleq \lfloor ((\tilde{i} + 1)D - \tau^+)/Q \rfloor$, given the current energy state s , after \tilde{i} EHBs, the *accumulated energy level* lies in the interval $\mathcal{A} \triangleq (s + \tilde{i}D^-, s + \tilde{i}D)$ with positive probability distribution. Also we see that interval $\Delta \triangleq (\tilde{j}Q + \tau^- - D^-, \tilde{j}Q + \tau^+ - D) \subset \mathcal{A}$, thus, there is at least (because we have only considered the scenario that harvested energy by each EHB lies in $[D^-, D)$) a probability $q \triangleq \inf_{\tilde{x}} \int_{\tilde{x}} \tilde{f}_{\tilde{i}}(x)$, interval $\tilde{\tau} \subset \mathcal{S}$, length of $\tilde{\tau} = \text{length of } \Delta = \tau/2$ that the accumulated energy level lies in Δ . Therefore, after the next EHB with probability p that the harvested energy lies in $[D^-, D)$, the accumulated energy level lies in the interval $[\tilde{j}Q + \tau^-, \tilde{j}Q + \tau^+)$, which means that after the current state $\tilde{\xi}_j = s$, with \tilde{j} steps (each step consumes the amount of energy, Q), there is at least a probability, $q \times p$ to make the Markov chain hit the interval (τ^-, τ^+) . Thus, Markov chain $\tilde{\xi}_j$ is a positive recurrent Harris chain [30].

Step 2: In the aforementioned Markov chain, we still assume that the current state $\tilde{\xi}_j = s$. Thus, in the previous state, the available energy could be higher than Q , i.e., $\tilde{\xi}_{j-1} = s + Q$, and $\tilde{\xi}_{j-1}$ could also be smaller than Q , i.e., based on energy level $\tilde{\xi}_{j-1}$, there are i EHBs ($i = 1, 2, 3, \dots$) to make the energy level reach $Q + s$, which makes $\tilde{\xi}_j = s$. Based on the above and the Markovian property, the steady-state distribution of the process, $g(x)$, should satisfy the following conditions: (1) $\int_0^\infty g(x) = 1$ and (2) $g(x) = g(x + Q) + \sum_{i=1}^\infty \int_x^{Q+x} g_{i-1}(Q + x - y)f(y)dy$. where $g_i(x)$ represent the pdf of energy level after i EHBs following a ECB, which is given by

$$g_i(x) = \begin{cases} g(x), & i = 0, \\ \left(\underbrace{g \star f \star f \star \dots \star f}_i \right) (x), & i > 0. \end{cases} \quad (\text{A.2})$$

Because $f(x)$ and $g_i(x) \geq 0$ for all x and $i = 0, 1, 2, \dots$, by using Tonelli's theorem for sums and integrals [31], we exchange the summation and integral operator in Condition 2, thus we have

$$g(x) = g(x + Q) + \int_x^{Q+x} \left(\sum_{i=0}^\infty g_i(Q + x - y) \right) f(y)dy. \quad (\text{A.3})$$

Taking (A.1) into (A.2), we have

$$g_i(x) = \frac{1}{\rho} \left(\left(\underbrace{F \star f \star f \star \dots \star f}_{i-1 \text{ convolutions}} \right) (x) - \left(\underbrace{F \star f \star f \star \dots \star f}_i \right) (x) \right), i > 0. \quad (\text{A.4})$$

Since $0 \leq F(x) \leq 1$, $f(x) \geq 0$ and $\int_0^\infty f(x) = 1$, when $i \rightarrow \infty$, we have [30]

$$\left(\underbrace{F \star f \star f \dots \star f}_i(x) \right) \rightarrow 0. \quad (\text{A.5})$$

From (A.4) and (A.5), we have

$$\begin{aligned} \sum_{i=0}^{\infty} g_i(Q+x-y) &= \frac{1}{\rho} (1 - F(Q+x-y)) \\ &+ \frac{1}{\rho} (F(Q+x-y) - (F \star f)(Q+x-y)) \\ &+ \frac{1}{\rho} ((F \star f)(Q+x-y) - (F \star f \star f)(Q+x-y)) + \dots \\ &= \frac{1}{\rho} \left(1 - \lim_{i \rightarrow \infty} \left(\underbrace{F \star f \star f \dots \star f}_i(x) \right) \right) = \frac{1}{\rho}. \end{aligned} \quad (\text{A.6})$$

Taking (A.6) and (A.1) into the right side of (A.3), we have

$$\begin{aligned} g(x+Q) + \int_x^{Q+x} \left(\sum_{i=0}^{\infty} g_i(Q+x-y) \right) f(y) dy \\ &= \frac{1}{\rho} (1 - F(x+Q)) + \int_x^{Q+x} \frac{1}{\rho} f(y) dy \\ &= \frac{1}{\rho} (1 - F(x+Q)) + \frac{1}{\rho} (F(Q+x) - F(x)) \\ &= \frac{1}{\rho} (1 - F(x)). \end{aligned} \quad (\text{A.7})$$

Thus, $g(x)$ in (A.2) satisfies Condition 2. Because of $\int_0^\infty (1 - F(x)) = \mathbb{E}\{\xi_i\}$ [30], Condition 1 is also satisfied, yielding the desired result. ■

APPENDIX B PROOF OF LEMMA 1

For general random energy arrival processes, the proof is based on Lemma A1 given in Appendix A. First, we find an arbitrarily small Q which is a constant such that \mathcal{E}_{SB} and \mathcal{E}_{TB} are integer multiples of it. Then, from an energy perspective, we equivalently treat the proposed communication protocol with energy harvesting, sensing and transmission as a simple harvest-then-use process with EHBs and ECBs (each consumes energy, Q) as discussed in Lemma A1. Thus, the energy level after a TB, can be treated equivalently as that after a corresponding ECB. Therefore, the steady-state distribution of energy level after each TB is the same as that after each ECB, which is given in Lemma A1, completing the proof.

APPENDIX C EVENT AND RANDOM VARIABLE DEFINITIONS

To assist the proofs of the main results, we use UC to denote the sequence of time blocks from an arbitrary STB to the next

STB. Also we define two events (according to [30]) and several discrete random variables (r.v.s) for convenience:

- 1) Event Λ_{suc} : Given a SB, its generated information is successfully transmitted to the sink, i.e., STB occurs during the W blocks after the SB.
- 2) Event Λ_{fail} : Given a SB, its generated information is not successfully transmitted to the sink, i.e., STB does not occur during the W blocks after the SB.
- 3) r.v. N , $1 \leq N \leq W$: Given a SB, it is followed by N TBs before the next SB. I.e., if Λ_{suc} occurs, the N TBs includes $N - 1$ FTBs and one STB. While if Λ_{fail} occurs, all the N TBs are FTBs.
- 4) r.v. L , $1 \leq L \leq W$: After a SB, the L th block is the last TB before the next SB. I.e., if Λ_{suc} occurs, the L th block is a STB, thus L is the update age. While if Λ_{fail} occurs, the L th block is the last FTB during the time window for retransmissions, W .
- 5) r.v. \tilde{V} , $\tilde{V} \geq -1$: Given a SB, if Λ_{suc} occurs, $\tilde{V} = -1$, while if an Λ_{fail} occurs, \tilde{V} is the number of the required EHBs after the time window for retransmissions, W , in order to harvest the amount of energy, \mathcal{E}_{TB} . Note that, after a Λ_{fail} , the amount of energy $\mathcal{E}_{\text{SB}} + \mathcal{E}_{\text{TB}}$ is required to be reached in order to support the following SB and TB. Without loss of generality, here we assume that the energy harvesting process first meets the energy level \mathcal{E}_{TB} , and the TB consumes the energy, \mathcal{E}_{TB} , (V)irtually. From Lemma 1 and its proof, the steady-state distribution of the available energy level after the \tilde{V} EHBs is $g(\epsilon)$.
- 6) r.v. V , $V \geq 0$. Given a SB and conditioned on a Λ_{fail} occurs, V is the number of the required EHBs after the time window for retransmissions, W , in order to harvest the amount of energy, \mathcal{E}_{TB} . From the definition of V and \tilde{V} , it is easy to see that

$$\begin{aligned} \Pr\{V = v\} &= \Pr\{\tilde{V} = v | \Lambda_{\text{fail}}\} \\ &= \frac{\Pr\{\tilde{V} = v\}}{\Pr\{\Lambda_{\text{fail}}\}}, \quad v = 0, 1, \dots \end{aligned} \quad (\text{C.1})$$

- 7) r.v. $E(\mathcal{E})$, $E(\mathcal{E}) \geq 0$: Given the distribution of initial energy level, $g(\epsilon)$, and the amount of target energy, \mathcal{E} , the required number of energy harvesting block is $E(\mathcal{E})$. For a deterministic energy arrival process, straightforwardly we have

$$\Pr\{E(\mathcal{E}) = i\} = 1, \quad i = \mathcal{E}/\rho. \quad (\text{C.2})$$

For a general random energy arrival process, from the definition of $E(\mathcal{E})$, Lemma 1 and its proof, we have

$$\Pr\{E(\mathcal{E}) = i\} = G_{i-1}(\mathcal{E}) - G_i(\mathcal{E}), \quad i = 0, 1, 2, \dots \quad (\text{C.3})$$

where

$$G_i(x) = \begin{cases} 1, & i = -1, \\ \int_0^x g_i(u) du, & i \geq 0, \end{cases} \quad (\text{C.4})$$

and $g_i(x)$ is defined in (A.2).

For *exponential* energy arrival process, we know that the energy accumulation process during EHBs after a TB is a *Poisson* process [30], thus, we have

$$\begin{aligned} \Pr\{E(\mathcal{E}) = i\} &= G_{i-1}(\mathcal{E}) - G_i(\mathcal{E}) \\ &= \text{Pois}(i, \mathcal{E}/\rho), \quad i = 0, 1, \dots \end{aligned} \quad (\text{C.5})$$

8) r.v. M , $M \geq 0$: Given a UC, Λ_{fail} occur M times and followed by one Λ_{suc} in it.

From the definitions of event, we know that Λ_{suc} and Λ_{fail} are mutually exclusive events. Thus, we have

$$P_{\text{suc}} \triangleq \Pr\{\Lambda_{\text{suc}}\} \text{ and } \Pr\{\Lambda_{\text{fail}}\} = 1 - P_{\text{suc}}, \quad (\text{C.6})$$

where Λ_{suc} and Λ_{fail} depends on transmit outage probability in each TB, and the available energy after the first TB following the SB. Because we have assumed that the success of each transmission are independent of one another, and from Lemma 1, the distribution of the available energy after each TB is the same, each event $\Lambda_{\text{suc}}/\Lambda_{\text{fail}}$ is independent of one another during the communication process. Therefore, r.v. M follows the geometric distribution

$$\Pr\{M = m\} = P_{\text{suc}} (1 - P_{\text{suc}})^m, \quad m = 0, 1, 2, \dots \quad (\text{C.7})$$

APPENDIX D PMF OF UPDATE AGE

From the definitions in Appendix C, the pdf of T_{UA} can be calculated as

$$\Pr\{T_{\text{UA}} = k\} = \frac{\Pr\{L = k, \Lambda_{\text{suc}}\}}{\Pr\{\Lambda_{\text{suc}}\}}, \quad k = 1, 2, \dots, W. \quad (\text{D.1})$$

Using the law of total probability and the r.v.s defined in Appendix C, we have

$$\begin{aligned} \Pr\{L = k, \Lambda_{\text{suc}}\} &= \sum_{n=1}^k \Pr\{L = k, N = n, \Lambda_{\text{suc}}\} \\ &= \sum_{n=1}^k \Pr\{N = n, E((n-1)\mathcal{E}_{\text{TB}}) = k - n, \Lambda_{\text{suc}}\} \\ &= \sum_{n=1}^k \Pr\{N = n, \Lambda_{\text{suc}} | E((n-1)\mathcal{E}_{\text{TB}}) = k - n\} \\ &\quad \times \Pr\{E((n-1)\mathcal{E}_{\text{TB}}) = k - n\} \\ &= \sum_{n=1}^k (1 - P_{\text{out}}) (P_{\text{out}})^{n-1} \Pr\{E((n-1)\mathcal{E}_{\text{TB}}) = k - n\}. \end{aligned} \quad (\text{D.2})$$

Again using the law of total probability and using (D.2), (C.6) becomes

$$\begin{aligned} P_{\text{suc}} &= \Pr\{\Lambda_{\text{suc}}\} = \sum_{l=1}^W \Pr\{L = l, \Lambda_{\text{suc}}\} \\ &= \Pr\{L = 1, \Lambda_{\text{suc}}\} + \sum_{l=2}^W \Pr\{L = l, \Lambda_{\text{suc}}\} \\ &= 1 - P_{\text{out}} + \sum_{l=2}^W \sum_{n=2}^l \Pr\{L = l, N = n, \Lambda_{\text{suc}}\} \end{aligned}$$

$$\begin{aligned} &= 1 - P_{\text{out}} + \sum_{l=2}^W \sum_{n=2}^l \\ &\quad \Pr\{E((n-1)\mathcal{E}_{\text{TB}}) = l - n, N = n, \Lambda_{\text{suc}}\} \\ &= 1 - P_{\text{out}} + \sum_{l=2}^W \sum_{n=2}^l \\ &\quad \Pr\{N = n, \Lambda_{\text{suc}} | E((n-1)\mathcal{E}_{\text{TB}}) = l - n\} \\ &\quad \times \Pr\{E((n-1)\mathcal{E}_{\text{TB}}) = l - n\} \\ &= 1 - P_{\text{out}} + \sum_{l=2}^W \sum_{n=2}^l (1 - P_{\text{out}}) (P_{\text{out}})^{n-1} \\ &\quad \Pr\{E((n-1)\mathcal{E}_{\text{TB}}) = l - n\}. \end{aligned} \quad (\text{D.3})$$

By taking (C.2), (C.3) and (C.5) into (D.2) and (D.3), and then substituting (D.2) and (D.3) into (D.1), the pmfs of T_{UA} for deterministic, general random and exponential energy arrival process are given in Theorems 1, 2 and 3, respectively.

APPENDIX E PMF OF UPDATE CYCLE

First, assuming that Λ_{fail} occurs m times during a UC, we define r.v.s $E_0, V_i, E_i, i = 1, 2, \dots, m$, and \tilde{L} . E_0 is the number of EHBs at the beginning of the UC until the first SB occurs which follows the same pmf with r.v. $E(\mathcal{E}_{\text{SB}} + \mathcal{E}_{\text{TB}})$. V_i is the number of EHBs required to harvest the amount of energy, \mathcal{E}_{TB} , outside the time window for retransmissions of the i th Λ_{fail} . E_i is the number of EHBs required to harvest the amount of energy, \mathcal{E}_{SB} , following V_i EHBs after the i th Λ_{fail} . \tilde{L} is the number of blocks after a SB to the last TB before the next SB, and the TB is a STB. From the r.v. definitions in Appendix C, E_0, V_i and E_i follow the same distribution with r.v.s $E(\mathcal{E}_{\text{SB}} + \mathcal{E}_{\text{TB}})$, V and $E(\mathcal{E}_{\text{SB}})$, respectively, and

$$\Pr\{\tilde{L} = l\} = \Pr\{L = l, \Lambda_{\text{suc}}\}, \quad l = 1, 2, \dots, W. \quad (\text{E.1})$$

From Lemma 1, $E_0, V_i, E_i, i = 1, 2, \dots, m$, and \tilde{L} are mutually independent.

Then, the pmf of update cycle can be calculated as

$$\begin{aligned} \Pr\{T_{\text{UC}} = k\} &= \sum_m \Pr\{T_{\text{UC}} = k, M = m\} \\ &= \sum_m \Pr\{E_0 + E_1 + \dots + E_m + \tilde{V}_1 + \dots + \tilde{V}_m + m \times (1 + W) \\ &\quad + \tilde{L} + 1 = k, \tilde{V}_1, \tilde{V}_2, \dots, \tilde{V}_m \geq 0\} \\ &= \sum_{m=0}^{\hat{m}} \Pr\{E_0 + E_1 + \dots + E_m + \tilde{V}_1 + \dots + \tilde{V}_m + \tilde{L} = \\ &\quad k - m \times (1 + W) - 1, \tilde{V}_1, \tilde{V}_2, \dots, \tilde{V}_m \geq 0\}, \quad k = 2, 3, \dots, \end{aligned} \quad (\text{E.2})$$

where $\hat{m} = \left\lfloor \frac{k-2}{W+1} \right\rfloor$. For simplicity, we define the following discrete functions:

$$\begin{aligned}\zeta(\mathcal{E}, i) &\triangleq \Pr\{E(\mathcal{E}) = i\}, \quad i = 0, 1, 2, \dots \\ \iota(l) &\triangleq \Pr\{\tilde{L} = l\} = \Pr\{L = l, \Lambda_{\text{suc}}\}, \quad l = 1, 2, \dots, W \\ \vartheta(v) &\triangleq \Pr\{\tilde{V} = v\}, \quad v = 0, 1, \dots\end{aligned}\quad (\text{E.3})$$

where $\zeta(\mathcal{E}, i)$ and $\iota(l)$ are obtained directly from (C.2), (C.3), (C.5) and (D.2), respectively, and $\vartheta(v)$ will be derived later. Therefore, pmf of T_{UC} in (E.2) can be calculated as

$$\Pr\{T_{\text{UC}} = k\} = \sum_{m=0}^{\hat{m}} \left(\zeta(\mathcal{E}_{\text{SB}} + \mathcal{E}_{\text{TB}}) \underbrace{* \zeta(\mathcal{E}_{\text{SB}}) * \dots * \zeta(\mathcal{E}_{\text{SB}})}_{m \text{ convolutions}} \right. \\ \left. * \underbrace{\vartheta * \dots * \vartheta * \iota}_{m \text{ convolutions}} \right) (k - m(1 + W) - 1). \quad (\text{E.4})$$

Now we derive the expression for $\vartheta(i)$. From the definitions of r.v. in Appendix C, we have

$$\begin{aligned}\vartheta(v) &= \Pr\{\tilde{V} = v\} = \Pr\{\Lambda_{\text{fail}}, \tilde{V} = v\} \\ &= \sum_{n=1}^W \Pr\{\Lambda_{\text{fail}}, \tilde{V} = v, N = n\} \\ &= \Pr\{\Lambda_{\text{fail}}, \tilde{V} = v, N = 1\} + \sum_{n=2}^W \Pr\{\Lambda_{\text{fail}}, \tilde{V} = v, N = n\} \\ &= \Pr\{\Lambda_{\text{fail}}, \tilde{V} = v, N = 1\} \\ &\quad + \sum_{l=2}^W \sum_{n=2}^l \Pr\{\Lambda_{\text{fail}}, \tilde{V} = v, N = n, L = l\} \\ &= \Pr\{\Lambda_{\text{fail}}, N = 1, E(\mathcal{E}_{\text{TB}}) = W + v - 1\} \\ &\quad + \sum_{l=2}^W \sum_{n=2}^l \Pr\{\Lambda_{\text{fail}}, N = n, E((n-1)\mathcal{E}_{\text{TB}}) \\ &\quad = l - n, E(\mathcal{E}_{\text{TB}}) = W + v - l\} \\ &= \Pr\{\Lambda_{\text{fail}}, N = 1 | E(\mathcal{E}_{\text{TB}}) = W + v - 1\} \times \\ &\quad \Pr\{E(\mathcal{E}_{\text{TB}}) = W + v - 1\} \\ &\quad + \sum_{l=2}^W \sum_{n=2}^l \Pr\{\Lambda_{\text{fail}}, N = n | E((n-1)\mathcal{E}_{\text{TB}}) \\ &\quad = l - n, E(\mathcal{E}_{\text{TB}}) = W + v - l\} \\ &\quad \times \Pr\{E((n-1)\mathcal{E}_{\text{TB}}) = l - n, E(\mathcal{E}_{\text{TB}}) = W + v - l\} \\ &= P_{\text{out}} \Pr\{E(\mathcal{E}_{\text{TB}}) = W + v - 1\} \\ &\quad + \sum_{l=2}^W \sum_{n=2}^l (P_{\text{out}})^n \Pr\{E((n-1)\mathcal{E}_{\text{TB}}) = l - n\} \times \\ &\quad \Pr\{E(\mathcal{E}_{\text{TB}}) = W + v - l\}.\end{aligned}\quad (\text{E.5})$$

By taking functions (E.5), $\zeta(\mathcal{E}, i)$ and $\iota(l)$ in (E.3), into (E.4), and letting (C.2) and (C.3) substitute $\Pr\{E(\mathcal{E}) = i\}$, the pmf of T_{UC} for deterministic and general random energy arrival process can be calculated, respectively, as given in Theorems 4 and

5. While for the exponential energy arrival process, by using the sum property of Poisson distribution, we have

$$\Pr\{E(\mathcal{E}_1)_1 + E(\mathcal{E}_2)_2 = i\} = \Pr\{E(\mathcal{E}_1 + \mathcal{E}_2) = i\}, \quad (\text{E.6})$$

where $E(\mathcal{E}_1)_1$ and $E(\mathcal{E}_2)_2$ are two independent random variables which have the same distribution with $E(\mathcal{E}_1)$ and $E(\mathcal{E}_2)$ defined in Appendix C, respectively. Therefore, letting (C.5) substitute $\Pr\{E(\mathcal{E}) = i\}$, the pmf of T_{UC} for exponential energy arrival process can be further simplified as given in Theorem 6.

APPENDIX F AVERAGE UPDATE CYCLE

Based on Appendix E, average update cycle can be calculated as

$$\begin{aligned}\bar{T}_{\text{UC}} &= \mathbb{E}\{\mathbb{E}\{T_{\text{UC}}|M\}\} = \sum_{m=0}^{\infty} \Pr\{M = m\} \mathbb{E}\{T_{\text{UC}}|M = m\} \\ &= \sum_{m=0}^{\infty} \Pr\{M = m\} \mathbb{E}\{E_0 + E_1 + \dots + E_m \\ &\quad + V_1 + V_2 + \dots + V_m + m \times (1 + W) + 1 + T_{\text{UA}}\} \\ &= \sum_{m=0}^{\infty} \Pr\{M = m\} (\mathbb{E}\{E_0\} + \mathbb{E}\{E_1\} + \dots + \mathbb{E}\{E_m\} \\ &\quad + m \times \bar{V} + m \times (W + 1) + \bar{T}_{\text{UA}} + 1).\end{aligned}\quad (\text{F.1})$$

From Appendix E, we have

$$\mathbb{E}\{E_0\} = \frac{\mathcal{E}_{\text{SB}} + \mathcal{E}_{\text{TB}}}{\rho}, \quad \mathbb{E}\{E_i\} = \frac{\mathcal{E}_{\text{SB}}}{\rho}, \quad i = 1, 2, \dots, m. \quad (\text{F.2})$$

After taking (E.5) and (C.6) into (C.1) and some simplifications, the expectation of V can be calculated as

$$\begin{aligned}\bar{V} &= \sum_{v=0}^{\infty} v \frac{\vartheta(v)}{1 - P_{\text{suc}}} = \frac{P_{\text{out}}}{1 - P_{\text{suc}}} \left(\frac{\mathcal{E}_{\text{TB}}}{\rho} - \sum_{i=0}^{W-2} i \Pr\{E(\mathcal{E}_{\text{TB}}) = i\} \right. \\ &\quad \left. - (W-1) \left(1 - \sum_{i=0}^{W-2} \Pr\{E(\mathcal{E}_{\text{TB}}) = i\} \right) \right) \\ &\quad + \frac{1}{1 - P_{\text{suc}}} \sum_{l=2}^W \sum_{n=2}^l (P_{\text{out}})^n \Pr\{E((n-1)\mathcal{E}_{\text{TB}}) = l - n\} \\ &\quad \times \left(\frac{\mathcal{E}_{\text{TB}}}{\rho} - \sum_{i=0}^{W-l-1} i \Pr\{E(\mathcal{E}_{\text{TB}}) = i\} - (W-l) \right. \\ &\quad \left. \left(1 - \sum_{i=0}^{W-l-1} \Pr\{E(\mathcal{E}_{\text{TB}}) = i\} \right) \right).\end{aligned}\quad (\text{F.3})$$

By taking (F.2), (F.3) and (C.7) into (F.1), and further substituting P_{suc} and \bar{T}_{UA} given in Corollaries 1, 2 and 3, average update cycle for deterministic, general random and exponential energy arrival processes are given in Corollaries 5, 6 and 7, respectively.

APPENDIX G
ASYMPTOTIC LOWER/UPPER BOUNDS

From Corollaries 1 and 2, it is easy to see that \bar{T}_{UA} increase with W . While for \bar{T}_{UC} , the monotonicity is not explicitly observed from Corollary 6. Due to space limitations, a sketch of the proof is given: When W increases, more TBs are allowed, thus more STBs occurs during the communication process, which also means shorter average update cycle.

When $W \rightarrow \infty$, the sensed information in each SB will be successfully transmitted to the sink, i.e., Λ_{SUC} always occurs and $P_{SUC} \rightarrow 1$. Thus, UC contains the EHBs to harvest the amount of energy, $\mathcal{E}_{SB} + \mathcal{E}_{TB}$, the SB, and the blocks in T_{UA} . Based on this explanation, for the average update age, we have

$$\begin{aligned}
 \lim_{W \rightarrow \infty} \bar{T}_{UA} &= \sum_{n=1}^{\infty} \Pr\{N = n\} \mathbb{E}\{T_{UA}|N = n\} \\
 &= \sum_{n=1}^{\infty} (1 - P_{out}) (P_{out})^{n-1} \\
 &\quad \mathbb{E}\{n + E((n-1)\mathcal{E}_{TB})\} \\
 &= \sum_{n=1}^{\infty} (1 - P_{out}) (P_{out})^{n-1} \left(n + (n-1) \frac{\mathcal{E}_{TB}}{\rho} \right) \\
 &= 1 + (\mathcal{E}_{TB}/\rho + 1) P_{out}/(1 - P_{out}).
 \end{aligned} \tag{G.1}$$

For the average update cycle, we have

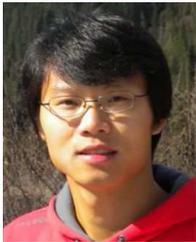
$$\begin{aligned}
 \lim_{W \rightarrow \infty} \bar{T}_{UC} &= \sum_{n=1}^{\infty} \Pr\{N = n\} \mathbb{E}\{T_{UC}|N = n\} \\
 &= \sum_{n=1}^{\infty} (1 - P_{out}) (P_{out})^{n-1} \mathbb{E}\{E(\mathcal{E}_{SB} + \mathcal{E}_{TB}) \\
 &\quad + 1 + n + E((n-1)\mathcal{E}_{TB})\} \\
 &= \sum_{n=1}^{\infty} (1 - P_{out}) (P_{out})^{n-1} \left(n + 1 + \frac{\mathcal{E}_{SB} + n\mathcal{E}_{TB}}{\rho} \right) \\
 &= 2 + (\mathcal{E}_{TB}/\rho + 1) P_{out}/(1 - P_{out}) + (\mathcal{E}_{SB} + \mathcal{E}_{TB})/\rho.
 \end{aligned} \tag{G.2}$$

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