A Fault-Tolerant Framework for Large-Scale Simulations

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outline

Background

- Faults and Fault-Tolerant Techniques (FT)
- Sparse Grids
- The Sparse Grid Combination Technique
- Complexity Metrics

Developing the Framework

- Building Sparse Grid Solvers
- Requirements
- Numerical MapReduce Framework (NuMRF)
- Parallel SGCT Implementation

Future Plans

- Integration into GENE
- Extension to Handling Soft Faults

fault recovery and fault-tolerance

Technological approaches:

- Replication/redundancy
- Runtime checkpointing with recovery through restart/task reassignment
- Runtime recreation of lost data using neighboring data



"...computational techniques for one mill...BILLION processing elements!"

Algorithm-based FT (ABFT):

- Huang and Abraham (1984): row/column checksums to correct for computational errors
- Du et al. (2012): checksum-based fail/stop in to LU & QR decompositions
- Liu (2002); Geist and Engleman (2007): chaotic relaxation
- Dean and Ghemawat (2004): MapReduce
- Our group: sparse grid combination method with built-in runtime fault-tolerance

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what is a sparse grid?

A solution to a complexity problem:

- The number of gridpoints on a *d*-dimensional isotropic grid grows exponentially w.r.t. *d*
- This is the curse of dimensionality
- A *sparse grid* provides fine-scale resolution in each dimension, but not combined fine scales from all multidimensional subspaces
- Constructed from a number of coarser *component grids* that are fine-scale in some dimensions but coarse in others
- Developed to solve problems in high dimensions





sparse grids reduce problem size dramatically



 $|\mathscr{F}| \propto 2^{Ld}$ $|\mathscr{S}| \propto 2^{L}L^{d-1}$ $R_{C} = \frac{|\mathscr{F}|}{|\mathscr{S}|} \propto \left(\frac{2^{L}}{L}\right)^{d-1}$

geometric definition of sparse grid

a simple sparse grid





sparse grid in frequency / scale space



captures fine scales in both dimensions but not joint fine scales

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The classic combination solution $f_L^C(\vec{x})$ for level *L* in *d* dimensions is, in terms of the component grid solutions $f_{\vec{l}}(\vec{x})$

$$f_L^C(\vec{x}) = \sum_{q=0}^{d-1} (-1)^q \binom{d-1}{q} \sum_{|\vec{l}|_1 = L-q} f_{\vec{l}}(\vec{x})$$

- Possible to include $m \le L 1$ hyperplanes' worth of "spare" component grids for FT.
- These spare grids are used only in scenarios of loss of one ore classic combination component grids due to fault(s)

classic combination and example ft scenarios



classic combination

loss of (3, 4)

loss of (2,5)

algorithm

- $\textbf{0} \ \ \mathsf{Pick} \ \ \mathsf{a} \ \ \mathsf{set} \ \ \mathcal{G} \ \ \mathsf{of} \ \ \mathsf{multidimensional}, \ \mathsf{coarser} \ \ \mathsf{component} \ \mathsf{grids}$
- **2** Solve on each component grid $\mathscr{G}_{\vec{l}}$ (interpolate to \mathscr{S})
- (Linear) Combination of component grids' solutions for solution on ${\mathscr S}$
- Optional: interpolate solution from \mathscr{S} to \mathscr{F}
- Some Evolution/Iteration: propagate solution on S back to each G_ℓ ∈ G
 - Error bounds for solutions on the sparse grid can be computed based on the scheme used on the component grids and the combination method
 - Each combination involves an $M \times N$ transfer

what is an $M \times N$ transfer?



Data connections for the 2D level 5, SGCT = >

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complexity analysis tells us...

- Lossy ABFT overhead is low compared to replication
- High values of (L, d) will engender
 - numerous component grid tasks
 - high grid data volumes
 - many (parallel) data connections routing data to/from the sparse grid
- Further modeling required using application- and platform-specific information
 - application performance data
 - hardware characteristics: processor speed, switch latency/bandwidth

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implications for a parallel sgct, cont'd...

requirements for a parallel sgct system

- Low-level automation:
 - Distributed grid/field data description
 - Parallel $M \times N$ transfer $\mathscr{G}_{\vec{l}} \leftrightarrow \mathscr{S}$
 - Data transformation (specifically, interpolation)
 - Performance measurement/timing
 - Fault detection/reporting
- High-level automation:
 - Scheduling of iterative execution of large numbers of tasks
 - Load balance based on task cost model (TCM)
 - Probabilistic Fault Detection (PFD) through predicted/elapsed runtime comparison
 - Automatic coordination of large numbers of $M \times N$ transfers
 - Monitoring/ explicit fault detection
 - Self-steering using an error quality of service (QoS) model to compute alternative solutions in the event of faults
- Compatibility with legacy science/engineering codes



python grids and fields toolkit (PyGrAFT)

PyGrAFT is the data language for NuMRF. It is a system for

- Representing logically Cartesian grids CartGrid class)
 - Arbitrary dimensionality supported
- Field data residing on these grids (GriddedScalarField)
 - Implemented using NumPy ndarray
 - Arbitrary dimensionality supported
 - Any NumPy base type supported
 - Any number of fields may be associated with a CartGrid
 - Complete flexibility regarding storage order
- Expressing multi-resolution relationships (FullGrid and ComponentGrid subclasses)
- Performing combinations involving component grids.
- Parallelization currently underway

At present, there are numerous test examples. Including generation of most of the sparse grid pictures in this talk.

PyGrAFT: Comparison of FT Techniques on 3D Advection

- Problem size L = 21, truncation parameter 5, combine 4 times; MTF: 25...1000s
- Local checkpoint: each process saves copy of component grid
- Global checkpoint: each process keeps copy of last combined grid
- Recombine: avoid using data from failed processes



time vs. faults for 3D advection

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c++ parallel sgct implementation

- Implemented in three C++ classes:
 - GridCombine2D: Overall combination method
 - Vec2D: Supports fundamental calculations
 - ProcGrid2D: Domain decomposition for each grid

Level of abstraction reduced code complexity dramatically!

- Assumptions:
 - Each component grid $\mathscr{G}_{\vec{l}}$ is distributed over a 2D grid of MPI PE's $P_{\vec{l}}$
 - Algorithm uses gather-scatter within each grid's pool
 - Load balance computed with an awareness of computational cost; based on component grids' respective (fixed) Δt
- Implemented using aggressive defensive programming techniques (cross-checking 2D vector calculations, etc)
 - Robustness (simplest L = 4 case requires 32 processes!)
 - Rapid development
- Source only about 1000 lines of code
- Interoperable with NuMRF via CTypes

	Execution Ti	Normalized		
Cores	simulateAdvection	SGCT	Total	Efficiency
11	54.95	42.40	97.35	100.00
22	28.38	20.95	49.33	98.67
44	14.66	10.41	25.07	97.08
88	6.93	5.36	12.29	99.01
176	3.73	2.44	6.17	98.61
352	1.81	1.32	3.13	97.19
704	0.92	0.80	1.73	87.92
1408	0.45	0.59	1.04	73.13
2816	0.33	1.09	1.42	26.78

Fixed Dt, Level 4, grid points $(2^{12} + 1) \times (2^{12} + 1)$, number of combinations 100, number of time-steps 2^{12} , RAIJIN cluster.

	Execution Ti	Normalized		
Cores	simulateAdvection	SGCT	Total	Efficiency
17	27.87	22.36	50.24	100.00
34	14.60	11.21	25.81	97.33
68	7.31	5.54	12.84	97.82
136	3.63	2.70	6.33	99.21
272	1.79	1.67	3.46	90.75
544	0.92	1.07	1.99	78.89
1088	0.50	0.72	1.22	64.34
2176	0.41	1.19	1.60	24.53
4352	0.69	3.46	4.15	4.73

Non-fixed dt, Level 4, grid points $(2^{12} + 1) \times (2^{12} + 1)$, number of combinations 100, number of time-steps 2^{12} , RAIJIN cluster.

c++ parallel sgct performance analysis



Application total task Application MPI task Load balance for level 4, grid points $(2^{10} + 1) \times (2^{10} + 1)$, non-fixed dt, number of combinations 1, number of time-steps 2^{10} , OPL cluster

- Parallel SGCT has considerable complexity!
- NuMRF, a MapReduce variant: numerical-analysis-friendly, error/fault aware calling framework
- Implementation of NuMRF's data model (PyGrAFT) is well underway, with encouraging preliminary results
 - SGCT has considerably less overhead than in-memory local or global checkpointing
- A robust parallel SGCT has been built
 - Scaling is reasonable: depends on frequency of grid recombination and # cores
- Careful management of software complexity has been an essential part in the design of the framework.

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- Fault-Tolerant GENE gyro-kinetic plasma application
 - Using L = 4 3-D SGCT on $x \times ky \times z = 1024 \times 512 \times 32$ grid
 - Robust to process failure using ULFT on MPI 3.1
- Develop Infrastructure to deal with node failures.
- Completion of PyGrAFT: Parallelization, $M \times N$ services, interpolation services, and sparse grid representation
 - Integration of parallel SGCT C++ codes
 - Bandwidth-reducing optimization using hierarchical basis sub-grids
- Major follow-up project: soft error detection and avoidance
 - Based on wavelet analysis on SG hierarchical basis grids
 - Advantage: general technique, oblivious of details of simulation
 - Limitation: MTF must be > period of check + partial SGCT

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THANK YOU!

QUESTIONS?

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